# Bonding in Phosphineborane and Phosphine Oxide: an Ab initio SCF-LCAO-MO Study 

By J. Demuynck and A. Veillard*<br>(Institut de Chimie, 1, rue Blaise Pascal-67-Strasbourg, France)

Summary From ab initio SCF-MO calculations, $d$-orbital participation and $\pi$-back-donation appears important in $\mathrm{PH}_{3} \mathrm{O}$ but rather small in $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$.

There is much speculation concerning the nature of the co-ordinate bonding by the phosphine molecule $\mathrm{PH}_{3}$. Two simple adducts of this molecule are the phosphineborane molecule $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}{ }^{1}$ and the hypothetical phosphine
geometries: $\mathrm{P}-\mathrm{H}$ bond length $1 \cdot 420 \AA$ (experimental value in $\mathrm{PH}_{3}{ }^{7}$ ), $\mathrm{P}-\mathrm{B}$ bond length $\mathrm{I} .93 \AA$ (experimental value ${ }^{8}$ ), $\mathrm{P}-\mathrm{O}$ bond length $1.48 \AA$ (experimental value in $\mathrm{Me}_{3} \mathrm{PO}^{9}$ ), $\mathrm{B}-\mathrm{H}$ bond length $\mathrm{I} \cdot 19 \AA$ (average $\mathrm{B}-\mathrm{H}$ bond length ${ }^{10}$ ). All angles were assumed to be tetrahedral: this assumption appears reasonable on the basis of the experimental values for the C-P-C and C-P-O angles, respectively $106^{\circ}$ and $112^{\circ}$. in trimethylphosphine oxide. ${ }^{9}$

|  | $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$ | $\mathrm{PH}_{3} \mathrm{O}$ | $\mathrm{PH}_{3}$ | $\mathrm{BH}_{3}$ |
| :---: | :---: | :---: | :---: | :---: |
| Total energy (a.u.) | -368.8480 | -417.3168 | -342.4382 | $-26.3521$ |
| Dipole moment ( ${ }^{\text {d }}$ | 5.51 | $4 \cdot 74$ | $1 \cdot 11$ | 1.04 |
| Atomic populations |  |  |  |  |
| P 3s | $1 \cdot 46$ | 1.20 | $1 \cdot 54$ |  |
| $3 p_{\sigma}$ | 1.26 | 0.74 | $1 \cdot 67$ |  |
| $3 p \pi$ | 1.70 | $1 \cdot 62$ | 1.56 |  |
| $3 d_{\sigma}$ | $0 \cdot 08$ | $0 \cdot 14$ | 0.06 |  |
| $3 d_{\pi}$ | 0.05 | $0 \cdot 22$ | 0.03 |  |
| Total | 14.55 | 13.92 | 14.87 |  |
| X $2 s$ | 0.75 | 1.84 |  | 0.86 |
| $2 p_{\sigma}$ | $0 \cdot 46$ | 1-34 |  | $0 \cdot 01$ |
| $2 p_{\pi}$ | $1 \cdot 64$ | $3 \cdot 50$ |  | 1.72 |
| Total | $4 \cdot 86$ | 8.72 |  | $4 \cdot 58$ |
| $\mathrm{H}_{\mathrm{P}} \mathrm{l} s$ | 1.00 | $1 \cdot 10$ | 1.02 |  |
| Total | 1.02 | 1-12 | $1 \cdot 04$ |  |
| Hx ${ }^{\text {s }}$ | $1 \cdot 16$ |  |  | 1.12 |
| Total | $1 \cdot 18$ |  |  | $1 \cdot 14$ |
| Overlap populations |  |  |  |  |
| P-X ( $\sigma$ ) | 0.458 | $0 \cdot 586$ |  |  |
| P-X ( $\pi$ ) | $0 \cdot 100$ | $0 \cdot 646$ |  |  |
| $\mathrm{P}-\mathrm{X}$ (Total) | 0.558 | 1-232 |  |  |
| 3 s 2 s | -0.022 | -0.097 |  |  |
| $3 p_{g}$ 2s | 0.018 | 0.007 |  |  |
| $3 d_{\sigma} \quad 2 s$ | 0.006 | 0.025 |  |  |
| $3 p \pi \quad 2 p \pi$ | 0.084 | 0.438 |  |  |
| $3 d_{\pi} \quad 2 p \pi$ | 0.016 | $0 \cdot 190$ |  |  |
| $3 \mathrm{~s} \quad 2 p_{\sigma}$ | 0.200 | $0 \cdot 239$ |  |  |
| $3 p^{2} \quad 2 p^{\prime}$ | $0 \cdot 244$ | 0.343 |  |  |
| $3 d_{\sigma} \quad 2 p_{\sigma}$ | $0 \cdot 012$ | $0 \cdot 057$ |  |  |

oxide molecule $\mathrm{PH}_{3} \mathrm{O} .{ }^{2}$ The importance of $3 d$-orbitals in phosphorus bonding has been a controversial question for a long time and, for instance, it has been assumed that the co-ordination in $\mathrm{PF}_{3} \cdot \mathrm{BH}_{3}$ is enhanced by back-donation to the phosphorus empty $d$-orbitals. ${ }^{3}$ Much discussion has been devoted to the nature of the $\mathrm{P}-\mathrm{O}$ bond in phosphoryl molecules, whether it is best considered as a $\mathrm{P}=\mathrm{O}$ double bond or as a $\sigma$-dative bond with some $\pi$-back-bonding. ${ }^{4}$

We report here the results of $a b$ initio SCF-LCAO-MO calculations for the $\mathrm{PH}_{3} \mathrm{O}$ and $\mathrm{PH}_{3} \mathrm{BH}_{3}$ molecules, together with calculations for the parent compounds $\mathrm{PH}_{3}$ and $\mathrm{BH}_{3}$ (in a tetrahedral conformation). We used a basis set of twelve $s$ and nine $p$ Gaussian functions on phosphorus, ${ }^{5}$ ten $s$ and $\operatorname{six} p$ functions on boron and oxygen, ${ }^{6}$ five $s$ functions on hydrogen; ${ }^{6}$ to these orbitals, a set of $d$ functions on P (exponent 0.55 ) and on $O$ (exponent $1 \cdot 0$ ), a $d_{x z}$ and $d_{y z}$ function on $B$ (exponent $1 \cdot 0$ ), and a set of $p$ functions on $H$ (exponent $0 \cdot 8$ ) have also been added. $\dagger$

Calculations have been performed with the following
$\dagger$ The ternary axis of the molecules has been taken as the $z$-axis.

The results are summarised in the Table. As a test of the quality of our wave functions, we shall first compare our results for the phosphine molecule with those reported recently. ${ }^{11}$ The basis set used in ref. 11 differs from our basis set only by the use of two sets of $d$ functions. The corresponding energy value for a tetrahedral angle (pyramid height of $0.47 \AA$ ) is -342.440 a.u., slightly lower than our value. The corresponding values for the dipole moment, the phosphorus $3 d$ population, and total population are $0.90 \mathrm{D}, 0.17$, and 14.85 , to be compared with our values of $1 \cdot 11 \mathrm{D}, 0.09$, and $14 \cdot 87$. Apart from a slight reduction in the $d$ orbital population due to the use of only one set of $d$ functions, our results are very close to the one reported by Lehn and Munsch.

A much debated question is the $d$-orbital participation in phosphorus compounds. From the Table, it is apparent that this participation is much more important in $\mathrm{PH}_{3} \mathrm{O}$ than in $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$ or in $\mathrm{PH}_{3}$. The $d$-orbital population is 0.09 in $\mathrm{PH}_{3}$ and 0.13 in $\mathrm{PH}_{3} \mathrm{BH}_{3}$, but rises to 0.36 in $\mathrm{PH}_{3} \mathrm{O}$

Most of the $3 d$ population in $\mathrm{PH}_{3} \mathrm{O}$ is of $3 d_{\pi}$ type, while it is of $3 d_{\sigma}$ type in $\mathrm{PH}_{3}$ and $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$. The $d$-orbital participation is also apparent from the overlap populations. The contribution of phosphorus $3 d$-orbitals to the overlap population for the $\mathrm{P}-\mathrm{X}$ bond ( $\mathrm{X}=\mathrm{B}$ or O ) is only 0.034 in $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$ but rises to 0.272 in $\mathrm{PH}_{3} \mathrm{O}$.

Examination of the overlap population reveals some important differences in the nature of the $\mathrm{P}-\mathrm{B}$ and $\mathrm{P}-\mathrm{O}$ co-ordinate bonding. In both molecules, there is an appreciable $\sigma$-bonding between the $3 s$ and $3 p_{\sigma}$ orbitals of phosphorus and the $2 p_{\sigma}$ orbital of boron or oxygen. In addition, there is in $\mathrm{PH}_{3} \mathrm{O}$ a significant $\pi$-bonding between the $3 p_{\pi}$ and $3 d_{\pi}$ orbitals of phosphorus and the $2 p_{\pi}$ orbital of oxygen. Such $\pi$-bonding is much weaker in $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$. This $\pi$-bonding and the correlative participation of phosphorus $3 d$-orbitals may be correlated with the $\pi$-donor ability of the co-ordinated group, the borane group being a very poor donor and the oxygen atom a relatively good one. A similar conclusion has been reached by Hillier and Saunders in a discussion of the bonding for the ligands $\mathrm{PF}_{3}$ and $\mathrm{PMe}_{3} .{ }^{12}$

Some insight into the nature of the co-ordinate bonding is also given by an examination of the charge transfer. The formal charge of the phosphorus atom is +0.13 in $\mathrm{PH}_{3},+0.45$ in $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$, and +1.08 in $\mathrm{PH}_{3} \mathrm{O}$, the charge of the boron atom is -0.42 in $\mathrm{BH}_{3}$ and -0.14 in $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$ and the charge of the oxygen atom -0.72 in $\mathrm{PH}_{3} \mathrm{O}$. This indicates that the charge transfer in $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}$ is relatively small, about 0.3 e , which is of the same order of magnitude as in $\mathrm{NH}_{3} \cdot \mathrm{BH}_{3} \cdot{ }^{13}$ The $\pi$-charge-transfer is negligible and most of the $\sigma$-charge-transfer goes from the $3 p_{z}$ orbital of phosphorus to the $2 p_{z}$ orbital of boron. The large charge-transfer in $\mathrm{PH}_{3} \mathrm{O}$ is the result of a large $\sigma$ -charge-transfer of about $1 \cdot 2 \mathrm{e}$ towards oxygen and of a smaller $\pi$-back-donation from the oxygen atom towards the phosphine group of about 0.5 e . In the three compounds $\mathrm{PH}_{3} \cdot \mathrm{BH}_{3}, \mathrm{NH}_{3} \cdot \mathrm{BH}_{3},{ }^{13}$ and $\mathrm{NH}_{3} \mathrm{O}^{14}$ which exhibit no backdonation, the computed dipole moments are very close, respectively $5 \cdot 5,5 \cdot 8$, and $5 \cdot 7 \mathrm{D}$. In $\mathrm{PH}_{3} \mathrm{O}$, this value is decreased to 4.7 D by back-donation of $\pi$-electrons.
(Received, May 18th, 1970; Com. 763.)
${ }^{1}$ R. W. Rudolph, R. W. Parry, and C. F. Farran, Inorg. Chem., 1966. 5, 723.
${ }^{2}$ E. Wiberg and G. Müller-Schiedmayer, Z. anorg. Chem., 1961, 308, 352.
${ }^{3}$ W. A. G. Graham and F. G. A. Stone, J. Inorg. Nuclear Chem., 1955, 3, 164.
${ }^{4}$ R. F. Hudson, Adv. Inorg. Chem. Radiochem., 1963, 5, 347.
${ }^{5}$ A. Veillard, Theor. Chim. Acta, 1968, 12, 405.
${ }^{6}$ S. Huzinaga, J. Chem. Phys., 1966, 45, 2593.
${ }^{7}$ C. A. Burrus, A. Jacke, and W. Gordy, Phys. Rev., 1954, 95, 700.
${ }^{8}$ E. L. McGandy, Diss. Abs., 1961, 22, 754.
${ }^{9}$ H. K. Wang, Acta Chem. Scand., 1965, 19, 879.
${ }^{10}$ "Interatomic Distances," Chem. Soc. Special Publ. No. 11, (1958).
${ }^{11}$ J. M. Lehn and B. Munsch, Chem. Comm., 1969, 1327.
${ }^{12}$ I. H. Hillier and V. R. Saunders, Chem. Comm., 1970, 316.
${ }^{13} \mathrm{~A}$. Veillard and R. Daudel, Colloque International du C.N.R.S. No. 191, "La nature et les propriétés des liaisons de co-ordination," Paris, 1969.
${ }_{14}$ P. Millie and G. Berthier, Colloque International du C.N.R.S. No. 191, Paris, 1969.

